

Using Schematically Heterogeneous Structures

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Abstract

Schematic heterogeneity arises when information that is represented as data under one schema, is represented within the schema (as metadata) in another. Schematic heterogeneity is an important class of heterogeneity that arises frequently in integrating legacy data in federated or data warehousing applications. Traditional query languages and view mechanisms are insufficient for reconciling and translating data between schematically heterogeneous schemas. Higher order query languages, that permit quantification over schema labels, have been proposed to permit querying and restructuring of data between schematically disparate schemas. We extend this work by considering how these languages can be used in practice. Specifically, we consider a restricted class of higher order views and show the power of these views in integrating legacy structures. Our results provide insights into the properties of restructuring transformations required to resolve schematic discrepancies. In addition, we show how the use of these views permits schema browsing and new forms of data independence that are important for global information systems. Furthermore, these views provide a framework for integrating semi-structured and unstructured queries, such as keyword searches, into a structured querying environment. We show how these views can be used with minimal extensions to existing query engines. We give conditions under which a higher order view is usable for answering a query and provide query translation algorithms.

1 Motivation

Two schemas are *schematically heterogeneous* if data under one schema corresponds to database or schema labels in the other. Schematic heterogeneity arises frequently since names for schema constructs (labels within schemas) often capture some intuitive semantic information. Some authors argue that even within the relational model it is more the

rule than the exception to find data represented in schema constructs [22]. Within semantic or object-based data models it is even more common [20]. For example, a stock class may have a set of subclasses, one for each company, where the names of companies serve as labels for the subclasses. Traditional query languages, including SQL and common object languages are typically not sufficient for reconciling schematic heterogeneity [22]. As a result, traditional query languages have limited use in creating integrated views of schematically disparate structures.

1.1 The Problem

We begin by considering a number of scenarios in which schematic heterogeneity can occur. The first is a classical problem in which a number of legacy sources, which differ schematically, must be used in concert. We then consider situations in which the source data is schematically consistent, but the ability to introduce schematically disparate views of the data can provide useful functionality. Our examples draw from the worlds of database publishing, data warehousing, and techniques for providing physical data independence.

1.1.1 Legacy System Integration

Consider a company wishing to integrate a number of legacy systems that manage or use information about stock prices. Each of the legacy systems was developed independently to meet the needs of different applications and may contain information about overlapping subsets of stock data. The company may now have a new application that requires access to all of this data. Due to the use of different design methodologies or the individual perspectives of various database designers, different decisions may have been made as to what data is invariant and therefore suitable for inclusion as part of a schema. An example of this, adapted from [22], is shown in Figure 1 depicting three relational schemas for stock information. All three schemas intuitively model similar information about the prices of company stocks on different dates. Schema S1 contains a single relational table. A table entry (tuple) contains a company name, a date, and the price of the company's stock on that date. Schema S2 contains a separate relational table for each company. Company names serve as labels for the tables. Schema S3 contains a single table where for each date the price of a company's stock is recorded in a separate attribute. In Schema S3, the company names serve as labels for a set of attributes each containing price information. Information that is cap-

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tured by data in the first schema (as values in a specific schema instance) is expressed within the schema itself (as either names of tables or names of attributes) in the second and third schemas.

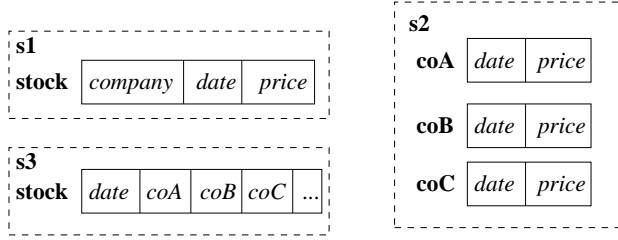


Figure 1: Three stock schemas. Table names are in bold, attribute names in italics.

Migrating all data to a common form would require that existing applications be rewritten which, for even moderately sized systems, is simply not feasible [6]. Neither is it feasible to require all new applications to use the current view(s) of stock data. Using Schemas S2 and S3, traditional query languages would not permit the expression of queries that quantified over company names (such as “find all companies whose stock price has ever gone over \$100”.) Hence, the schema design itself can limit the set of expressible queries. These limits may be unexceptionable for new applications.

Instead, we would like to construct a view (according to the modeling requirements of our new application) that can nevertheless be used to access the unchanged legacy stock data. The view must be data independent. That is, it should not depend on the specific names or numbers of companies and should not need to change as the data evolves.

Using SQL, a single data independent view cannot be constructed. Since SQL does not permit quantification over relation or attribute names, any SQL view would have to include company names as constants. The view $v1$ of Figure 2, which translates data from Schema $s2$ to $s1$, illustrates this. If the set of company names changes, the view definition would need to be altered. To permit the specification of data independent views, a language that permits quantification over schema labels is needed. Many higher order languages that include some form of quantification over schema constructs have been proposed. These include multi-database languages [27], logics [11, 23], algebras [33, 17], and object-

```

create view v1 (co, date, price) as
( select 'coA', date, price
  from coA
  union
  select 'coB', date, price
  from coB
  union
  select 'coC', date, price
  from coC
  ... )

create view v2 (co, date, price) as
select R, T.date, T.price
from s2->R, R T

create view v3 (co, date, price) as
select A, T.date, T.A
from s3::stock->A, S3::stock T
where A ≠ 'date'

```

Figure 2: Example SQL and SchemaSQL views.

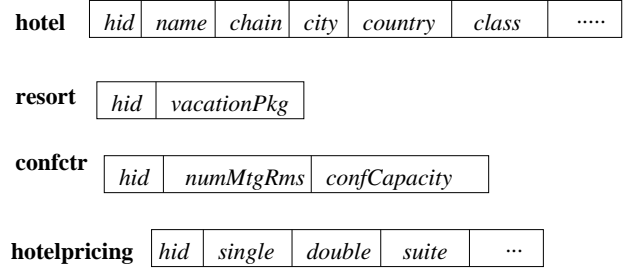


Figure 3: Hotel Database.

oriented languages [22, 4, 20] to name just a few. Views $v2$ and $v3$ of Figure 2 are examples of higher order views constructed using SchemaSQL [24], a higher order extension of SQL that permits quantification over database, relation and attribute names. In the view $v2$, the notation $s2 \rightarrow R$ declares R to be a relation variable ranging over all relations in $s2$. The variable T is a tuple variable declared to range over the relations of R . This view translates data from Schema $s2$ to Schema $s1$ and is independent of the specific relations present in $s2$. In the view $v3$, the declaration $s3 :: stock \rightarrow A$ declares the variable A to be an attribute variable ranging over all attribute names in the relation *stock* of Schema $s3$. The variable T is again a tuple variable, here declared to range over the tuples of the *stock* relation. View $v3$ translates data from $s3$ to $s1$. This example motivates the need to be able to reconcile heterogeneous representations dynamically, a task that can be accomplished using higher order views.

1.1.2 Database Publishing

Higher order reasoning has numerous applications beyond reconciliation of differing design choices. Consider the hotel information of Figure 3 which is adapted from the DataWeb system [31]. DataWeb permits the publishing of structured databases providing sophisticated browsing and navigation techniques to enable naive users to locate useful information in a large, complex data collection. In this example, the attribute *hid* in the relations is a foreign key to *hotel.hid*. The tables *resort* and *confctr* represent subclasses of the *hotel* table containing attributes specific to each type of hotel. The information common to all hotels is vertically partitioned between the *hotel* table and the *hotelpricing* table. The latter contains a number of attributes related to the pricing of different room types.

Consider the construction of a database publishing application, such as DataWeb, that makes this information available on the Web. The schema is rather complex so a useful interface would necessarily permit some form of schema independent querying. For example, a keyword search interface would permit users to find hotels in the “Sofitel” franchise without knowing which table or attribute contained this information (name, chain, branch, owner, etc.) A forms interface might permit a user to request hotels with rooms for under \$70 without requiring the user to indicate (or understand) specific price related attributes over which this predicate should be applied. Consider how either of these queries would be specified. The keyword search is essentially the query *select the hid of tuples in any relation where some*

attribute value contains “Softel”. The inexpensive query is *select hid from hotelpricing where any attribute value is less than 70*. Both of these queries are higher order. Although the information in the hotel database does not contain any schematic discrepancies, the ability to answer queries over schema components could be used to support the schema independent querying required in this environment.

Suppose the information of Figure 3 has been collected in a data warehouse and consider a decision analysis application on this information. Specifically, assume the application will need to aggregate hotel information over different dimensions presenting a tabular (or data cube style [14]) summary to a user. An example query would be to find the number of hotels in each country of each class (including subtotals for all classes and all countries). Using this information, a user can “drill down” to specific data of interest by refining the dimensions over which aggregation is done (for example, viewing information aggregated by country, then by city). The concept of data dimensions is central to decision analysis applications. They provide the axes over which data can be “sliced and diced”. In the first generation of decision analysis systems, the dimensions were fixed [12]. Many recent systems permit the dynamic creation (of a potentially large numbers) of new dimensions [31]. In our hotel example, this means the addition of new hierarchies over which hotels can be aggregated. Dimensions may be represented by attributes or sets of attributes. An extensible analysis system requires the ability to reason over (a time varying) set of new dimensions. Specifically, it must be possible to permit the user to specify predicates that can be applied to any subset of dimensions.

1.1.3 Physical Data Independence

Indexing architectures often use views to describe index structures in order to permit the integration of new indexes (or access methods) into a query optimizer [8, 37]. Tsatalos et al [37] have developed a robust indexing architecture that makes use of restricted views containing only selection, projection and join operations. The views are used to describe a wide array of advanced indexing techniques. However, they point out that their techniques cannot be used to describe indexing over subclasses of a class. This is due to the lack of support for unions and for schema independent views. Consider the class *tickets* that contains information about traffic violations issued by the highway patrol which is adapted from [1]. The class *tickets* contains the attributes *tnum*, *lic*, *infr* describing the ticket number, license number and infraction code respectively. Information kept by each jurisdiction (a state or region within a state) is kept in a subclass whose name is the jurisdiction’s name. Each jurisdiction maintains information about tickets issued in its boundaries and in addition attempts (although perhaps not consistently) to maintain information about all tickets given to people holding licenses issued within its region. The definition of a B⁺-tree index keyed on the ticket infraction is given in Figure 4 using the notation from [37]. The index is defined over all jurisdictions. In [37], indices must be described using SQL views and as a result, the proposal cannot express or use indices over data dependent collections of tables (or classes). For example, indices over all subclasses of a class cannot be express [37]. Using higher order views, such indices can be expressed. However, to make use of these new indices in query processing, it must be possible to determine whether a view (index) can be used in answering a query. Furthermore, it must be possible to determine what portion

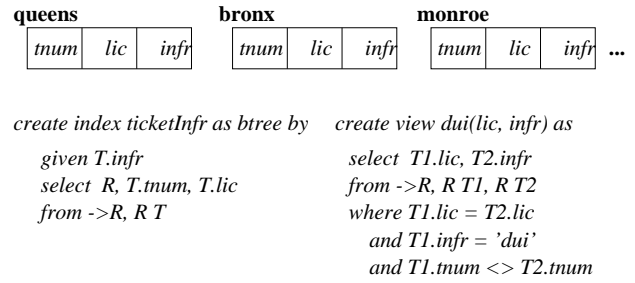


Figure 4: Traffic ticket database.

of a query the view (index) answers.

Using higher order views, a wide class of useful new indexing structures can be expressed. For example, consider the view *dui* of Figure 4 which can be used to describe an index helpful in evaluating *data fusion* [1] style queries. A data fusion query involves the self-join of a union of tables. The view *dui* finds all infractions issued to anyone with one or more ‘DUI’ infraction (driving under the influence of alcohol). This view may describe an index that materializes this specific fusion query.

Similarly, schematically disparate views of the data can be used to model an inverted index that might be used to support the evaluation of keyword search queries over a structured database. By incorporating such views into an architecture for supporting physical data independence, the query optimizer can reason about the use of these indexing structures and their combined used with traditional access methods.

1.2 Paper Overview

In this paper, we develop techniques such as those required in the above examples for understanding and managing schematic heterogeneity. Our examples point to several different scenarios in which some form of schematic reasoning is required. Indeed, the examples make use of higher order views, higher order queries and higher order indexes (schema independent indexes). On the surface, these examples seem to necessitate full support for a higher order query language and view definition facility capable of describing logical and physical (index) structures. Specifically, the examples point to the need for a language that is powerful enough to reconcile schematic heterogeneity and to describe heterogeneous data representations. Additionally, they point to the need for techniques to automatically translate queries against the view into queries against the legacy schema(s) and to optimize these modified queries.

Such extensions to a complex query processing engine can be prohibitively expensive. We therefore take a pragmatic approach. We propose a solution in which all schematic heterogeneity is reconciled by a limited form of higher order views called *dynamic views*.

In Section 2, we overview the contributions of this work and place it in the context of related work on schematic heterogeneity. In Section 3, we overview the proposed solution. While our solution does not provide full support for higher order reasoning, we show that it is still powerful enough to meet the needs of the diverse applications we have just outlined. In Section 4, we discuss the restructuring prop-

erties of dynamic views. In Section 5, we analyze when a dynamic view can be used to answer an SQL query and provide query translation algorithms. Given our desire to support data warehousing and database publishing applications, we include a discussion of aggregate queries and views in the analysis since such queries are important in these environments. In Section 6, we consider how dynamic views (whether used to describe legacy sources or indexes) can be used in a conventional query optimizer.

2 Related Work

The prevalence of schematic heterogeneity is well documented in the heterogeneous database research literature. The problem is discussed informally in early schema integration work with the goal of defining transformations between schematically disparate schemas [13] and in other work with the goal of enumerating and classifying the types of schematic differences that can arise [21, 18]. Builders of federated and warehousing systems frequently encounter schematic heterogeneity in practice. See the work on Garlic [7], TSIMMIS [10], and Pegasus [2] to name just a few. Work on managing and using schematically disparate structures has focussed on languages for querying such structures. MSQL provides basic features for querying over schema labels [27]. This and other higher-order query languages can be used in multi-database architectures where integration is not done *a priori* through an integrated view, but rather on demand in each query. More recently work on languages to query structured and semi-structured sources also provides higher-order capabilities [32].

Other proposals provide data model extensions to permit type extents (meta-extents) to range over unspecified collections [36]. New extents can be added dynamically without changing the schema (type) specification. Meta-extents are similar in motivation to the dynamic views we propose. However, dynamic views are more amenable to use in applications beyond integration, including those discussed in the introduction. Several proposals have considered the definition of higher order views for defining integrated views [22, 24]. We build on this work to consider how these views can be used in practice with minimal extensions to query processing engines.

3 Proposed Architecture

To present our solution, we will use SchemaSQL, a higher order extension of SQL [24]. We briefly overview the relevant features of SchemaSQL, defining the concept of *dynamic views* and *first order views* that will be central to our proposed solution. We then present our proposed architecture and show that it meets the needs of the applications outlined in Section 1.

3.1 SchemaSQL

SQL makes use of *tuple variables* that range over the tuples of a relation declared in the **from** clause of a query. *Domain variables* range over the values in a single attribute of a relation (for example, *stock.date*). SchemaSQL permits three additional types of variables: database, relation and attribute variables. The expression $\rightarrow D$ declares D to be a database variable ranging over all database names in a federation. The expression $db \rightarrow R$ declares R to be a relation variable ranging over all relations in db (which can be a constant or a database variable). The expression

$db :: rel \rightarrow A$, declares A to be an attribute variable ranging over all attribute names in the relation rel of database db . For clarity in our examples, we will use capital letters for variables (usually starting with D , R , A and T for database, relation, attribute and tuple variables respectively). Lower case strings will be used for specific database, attribute and relation names to help clarify the difference between variables and constants.

Attribute, relation, and database variables are collectively referred to as *schema variables*. Schema variables can appear in the query (select, from, group by, having, *etc.*, clauses) any where a domain variable can traditionally be used. In addition, SchemaSQL permits the specification of views that have data dependent output schemas. That is, the schema is defined by the query result. In SQL, the output schema is specified by labels (constants) in the **create view** clause. Specifically, one label is used for the relation name and one for each of the attribute names. We ignore shorthand notation permitted by SQL. In SchemaSQL, any of these labels may be replaced by variables. Examples are given in Figure 5. Views $v4$ and $v5$ translate data from Schema $s1$ of Figure 1 to Schemas $s2$ and $s3$, respectively. For clarity, we will explicitly define most domain variables in the from clause unless no confusion can arise. In the first view, data is grouped into different relations based on the value of the domain variable C . As this example shows, using variables for relation or database names, we can express data dependent unions (horizontal partitioning of a relation). In the second view, data is grouped into different tuples based on C and $date$. For a given date, $s3$ groups all stock prices for that date into a single tuple. If a company has multiple prices listed for the same date, then $s3$ will contain multiple tuples. Using variables for attribute names, we can express data dependent outer-joins (vertical partitioning of a relation). In this example, suppose $s1$ contains information about only two companies, coA and coB . Then $v5$ can be expressed as the following relational query, where \otimes denotes the full outer-join. The full semantics of these views is given elsewhere [24].

$$\begin{aligned} A &= \sigma_{company='coA'} stock \\ B &= \sigma_{company='coB'} stock \\ \Pi_{date, price}(A) &\otimes_{date} \Pi_{date, price}(B) \end{aligned}$$

If an instance of *stock* contains three price values for coA on 1/1/98 and two price values for coB on 1/1/98, then view $v5$ will contain the cross product of these values, or six tuples with the date 1/1/98.

In what follows, we will consider a restricted class of views with data dependent output schemas.

Definition 3.1 *A dynamic view is any SchemaSQL view that possesses a data dependent output schema defined by a query that uses only tuple and domain variables.*

In Figure 5, Views $v4$ and $v5$ are dynamic while $v6$ is not since it uses an attribute variable A . As we will show the restructuring properties of dynamic views are very powerful.

3.2 Architecture Definition

The requirements outlined in Section 1 necessitate the use of an integration that is independent of specific source structures. Under traditional integration paradigms [5], the integrated view depends directly on the source schemas. So we adopt the approach of [3, 26], in which the integrated schema

```

v4 create view s2::C(date, price) as
    select D, P
    from s1::stock T, T.company C,
        T.date D, T.price P

v5 create view s3::stock(date, C) as
    select D, P
    from s1::stock T, T.company C,
        T.date D, T.price P

```

```

v6 create view A::avg(date, avgprice) as
    select D, avg(P)
    from s3::stock T, s2::stock-> A, T.A P, T.date D
    where A ≠ 'date'
    group by A, D

```

Figure 5: Example SchemaSQL views with data dependent schemas.

is treated as a stable, central structure through which other evolving, dynamic data sources can be queried. That is, unlike traditional integration approaches, the integrated view is not synthesized from a snapshot of a set of local schemas. Rather, the integrated view is created to meet the requirements of the integration (for example, the decision analysis functions to be supported by a data warehouse). The local databases are treated as materialized views over the integrated schema. A query on the integration can be answered by rewriting it into a query on the local databases, using perhaps additional data that is stored directly under the integrated schema.

This choice of architecture is particularly appropriate for reconciling schematic discrepancies. Using a traditional synthesis approach the design choices of the current schemas (and the integration algorithm) will determine what data is “queriable” in the integration. In particular, data that is used as labels in all local sources will typically remain as part of the schema. Our architecture however, allows explicit choice as to how data and meta-data is divided. This choice can be made based on the requirements of the integration, rather than on legacy requirements they may not be valid for new applications. The architecture also permits data sources to evolve independent of the integration.

Using this approach, we restrict the integration schema and views as follows.

1. The integration schema I must be *first order*.

We will use the term *first order schema* (or view) for a schema under which all values of interest to a user are modeled as data. Hence, a schema is only first order relative to a given set of queries. For a set of queries Q , a schema is first order if all queries in Q can be written in a first order language such as SQL. This concept is closely related to *first order normal form* proposed in [28]. Schema $s2$ of Figure 1 may be first order for an application that does statistical analysis on individual company stocks and does not require the ability to issue queries that iterate over all companies.

While our solution will enable schema independent querying, such as keyword searching, it does not neces-

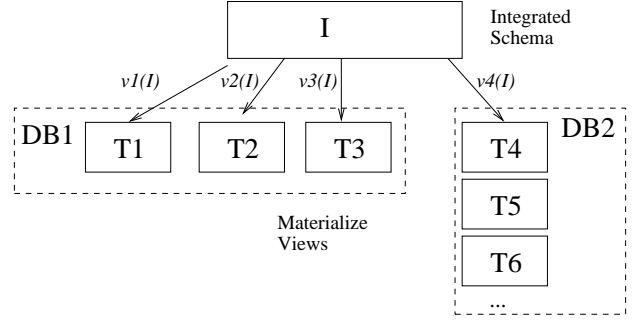


Figure 6: Integration Architecture.

itate that all schema components be made queriable. That is, the design of the integrated schema may limit which schema components from the sources may be queried.

2. All data sources are expressed as SQL or dynamic views on I .

Each local schema (or index) is described as a set of views on I . Let local schema $S = \{T_1, \dots, T_n\}$. Each T_j is a view on I , that is, $T_j = v_j(I)$ where v_j is an SQL or dynamic view. This architecture leaves open the possibility that a local schema may contain data (in other tables) that is not used in the integration. The integration may also contain locally stored data, not derived from one of the existing data sources.

This architecture is depicted graphically in Figure 6. Note that a single dynamic view may define a set of tables. Although we refer to I as an integration schema, it may in fact be a logical view on a homogeneous source. The view may be introduced to provide schema browsing functionality or new forms of physical data independence.

Within this framework, the dynamic view provides a natural barrier for encapsulating higher order reasoning. As we show, a query engine employing these views must be able to recognize when a view is usable in answering a query, but does not need full knowledge of the meaning of the higher order components of the view.

3.3 Applications

Despite its limitations, this restricted architecture can be used to address the requirements of the examples from Section 1. Recall the requirements these examples illustrated.

1. Cooperative querying of schematically heterogeneous structures.
2. Schema independent queries (and schema browsing).
3. Schema independent indexing.

We briefly revisit the examples of Section 1 and show how this architecture supports each application.

hprice	<i>hid</i>	<i>rmtype</i>	<i>price</i>
---------------	------------	---------------	--------------

create view *hotelpricing*(*hid*, *R*) as

```
select H, P
from hprice T, T.hid H, T.rmtype R, T.price P
```

Q select *H*
from *hprice* *T*, *T.price* *P*, *T.hid* *H*
where *P* < 70

Figure 7: Schema independent querying of *hotelpricing*.

Legacy System Integration The Schema *s1* can be used as the Integration I. All three schemas can then be represented as dynamic views on *I*. The mapping from *I* to *s1* is the identity map, and views *v4* and *v5* of Figure 5 provide the definitions for *s2* and *s3*. Queries posed on the integration must be translated to queries on the legacy schemas (materialized views). To do this, an algorithm for translating any SQL query into an SQL or SchemaSQL query on the underlying views is required. This algorithm will permit the answering of queries on the integration using data stored under the legacy sources.

Database Publishing Consider a query to retrieve inexpensive hotels where an inexpensive hotel is considered to be one that offers rooms for under \$70. The rooms may be of any type (single, double, suite, *etc.*) and the price may be valid any time (weekends, weekdays, off-season, *etc.*). On the schema of Figure 3, this query is `select hid from hotelpricing where any attribute value is less than $70`. To support this query, our architecture requires the use of an interface schema, like *hprice* of Figure 7. This schema represents the names of pricing attributes as data. Such a schema permits the expression of this query in SQL as shown in Query Q of Figure 7. The original *hotelpricing* table can be expressed as a dynamic view on this schema. To be evaluated, SQL queries on *hprice* must translated to SQL or SchemaSQL queries on the *hotelpricing* view.

Physical Data Independence Using the schema of Figure 8, the index and view of Figure 4 can be expressed as dynamic views. Recall that these structures could be used in evaluating data fusion style queries involving self-joins over large data-dependent unions of tables. The index and view are SQL views on the *tickets* tables. The original tables can be specified as a dynamic view on tickets (View V of Figure 8). If an SQL query on tickets can be answered entirely by using either the *ticketInfr* index or the *dui* view, then it can be translated into an SQL query on these structures. However, since these views do not fully replicate the source data, some queries may only be answered using the legacy sources (for example, a query to find all tickets issued to a specified license number). These queries can be translated into SQL or SchemaSQL queries on the legacy sources using View V.

In addition, dynamic queries can be used to model inverted indices that are useful in answering keyword search queries. An inverted index maps a keyword, for example “Sofitel”, to all tuples (or more generally documents) containing the keyword. In Figure 9, the table *hotelwords* con-

tickets	<i>state</i>	<i>tnum</i>	<i>lic</i>	<i>infr</i>
----------------	--------------	-------------	------------	-------------

create view *dui*(*lic*, *infr*) as

```
create index ticketInfr as btree by
given T.infr
select T.state, T.tnum, T.lic
from tickets T

select T1.lic, T2.infr
from tickets T1, tickets T2
where T1.lic = T2.lic and
T1.infr = 'dui' and
T1.tnum <> T2.tnum
```

V create view *S*(*tnum*, *lic*, *infr*) as
select *T.tnum*, *T.lic*, *T.infr*
from tickets *T*, *T.state* *S*

Figure 8: Ticket database.

tains for each hotel and for each attribute of a hotel, a tuple for each word or attribute value. The index *keywords* is an inverted index that given a specific keyword value returns a set of all hotel ids and corresponding attribute names that contain the keyword. Because the schema of *hotelwords* is first order, the inverted index is actually specified using an SQL view. However, it may be implemented as an actual inverted index on the materialize data in the table *hotel* of Figure 3.

Now consider a query to find all Sofitel hotels located in Athens. This query contains a structured predicate (*city* = “Athens”) and an unstructured predicate (\exists attribute *A* \wedge *A* = “Sofitel”). Specified on the *hotelwords* schema, this query is expressed in Figure 9. Note that the *keywords* index can be used to (partially) answer both predicates (and hence can answer the full query). The city predicate is only partially evaluated by the index so an additional selection (*attribute* = “city”) must be done. Similarly, the *hotel* view can be used to answer both predicates albeit only using a higher order query. In query planning, we would want to consider plans involving both views and to select a plan that most efficiently answers the query. Intuitively at least, this query can be more efficiently evaluated if the query processing engine recognizes that the structured predicate can be most efficiently answered by the *hotel* view and the unstructured predicate by the index and the results joined.

We have demonstrated how dynamic views, while limited by design, meet the requirements of a wide range of new, important applications. Furthermore, they provide a mechanism for integrating semi-structured or unstructured search style queries into the query planning of a traditional structured query optimizer. To do this, a schematically disparate view of (a possible schematically homogeneous) schema is introduced. This discussion has highlighted the remaining results required to use dynamic views in practice. Specifically, using this framework, the problem of answering queries over an integration *I* reduces to the problem of determining if a view or set of views *V* are usable in answering a query *Q* on *I* and finding an equivalent rewriting *Q'* on *V*.

4 Properties of Dynamic Views

In this section, we consider the problem of using dynamic views to answer SQL queries. The problem of using SQL views to answer SQL queries has been studied extensively.

hotelwords	hid	attribute	value
------------	-----	-----------	-------

create index keywords as inverted by
given value
select T.hid, T.attribute
from hotel

create view hotel (hid, A) as
select T.hid, T.value
from hotelwords T,
hotelwords.attribute A

Q select hid
from hotelwords T1, hotelwords T2
where T1.hid=T2.hid and T1.value = 'Sofitel'
and T2.attribute = 'city' and T2.value = 'Athens'

Figure 9: Keyword search query over hotels.

We make use of results by Srivastava et al [35] in which views and queries with aggregation and multi-set (bag) semantics are considered. These results generalize earlier work on conjunctive queries with set and multi-set semantics [25, 9]. We begin with a few definitions.

Definition 4.1 Queries $Q1$ and $Q2$ are set equivalent if they compute the same set of answers for any database.

Queries $Q1$ and $Q2$ are multi-set equivalent if they compute the same multi-set of answers for any database.

Definition 4.2 [35] A view V is set usable (respectively, multi-set usable) in Q if there exists a query Q' that is set equivalent (respectively, multi-set equivalent) to Q and Q' contains one or more occurrences of V .

4.1 Restructuring using SQL

To determining whether a dynamic view can be used to answer a query, it is necessary to understand the restructuring properties of dynamic views. The restructuring permitted by SQL can be broadly classified into two types. Reorganization and elimination of columns which is done using the join and project operators. Reorganization, summarization and elimination of tuples which is done using the select, join, grouping and aggregation operators.

For a view to be usable in answering a query, it must contain all the columns and all the tuples required by the query. The view must also not lose any associations between data values. Put another way, the view must not combine tuples that would not be combined in the original. In SQL, this last condition is checked by ensuring that the join conditions of the view match those of the query. However, for dynamic views some additional checking must be done. This is because the higher order functionality of the views permits a greater array of data restructuring than is possible with SQL.

db0 -- Integration

stock	exchange	company	date	price
-------	----------	---------	------	-------

coType	co	type
--------	----	------

db1

exch	eid	company	ibm	date	price
------	-----	---------	-----	------	-------

hp	date	price
----	------	-------

att	date	price
-----	------	-------

...

db2

nyse	date	price	ibm	price	ge	price	...
------	------	-------	-----	-------	----	-------	-----

Figure 10: Example views on a stock integration.

4.2 Restructuring using Relation and Database Variables

Relation and database variables permit the horizontal partitioning of data based on the value of an attribute. The restructuring properties provided by database variables is very similar to those of relation variables so in this discussion we only consider relation variables. For a table $r[a_0, a_1, \dots, a_n]$, the following is a simple dynamic view using a relation variable.

create view $A_0(a_1, a_2, \dots, a_n)$ as
select $T.a_1, T.a_2, \dots, T.a_n$
from r $T, T.a_0$ A_0

The query defining the view is an information capacity preserving mapping [30]. That is, for each instance of r there is a unique instance of the view. Intuitively, this means that the restructuring done to create the view does not lose any information [15]. We can use this intuition when considering whether a query can be answered using a dynamic view with a relation variable. The query defining the view may (and probably will) lose information, but the restructuring provided by the relation variable will not augment this loss.

Example 4.1 Consider Figure 11 containing the definition for the company tables of db1 and a Query $Q1$ on the Schema db0 of Figure 10. The Query $Q1$ finds companies that closed over 200 on two consecutive days since 1/1/98. Suppose we want to use db1 to answer $Q1$. $Q1'$ is a rewriting of $Q1$ using db1. We can use the formal properties of the view definition to show that $Q1$ and $Q1'$ are equivalent.

4.3 Restructuring using Attribute Variables

Attribute variables permit (data dependent) vertical partitioning of data based on the value of an attribute. For a table $r[a_0, a_1, \dots, a_n]$, the following is a simple dynamic view using an attribute variable.

```
create view db1::C(date, price) as
  select D, P
  from Db0::stock T, T.company C
  T.date D, T.price P
  where D > 1/1/90
```

Q1: select C1
 from db0::stock T1, db0::stock T2
 T1.company C1, T2.company C2
 where T1.date > 1/1/98 and
 T1.date = T2.date + 1 and
 T1.price > 200 and T2.price > 200
 and C1 = C2

Q1': select R1
 from db1-> R1, db1->R2 R1 T1, R2 T2
 T1.company C1, T2.company C2
 where T1.date > 1/1/98 and
 T1.date = T2.date + 1 and
 T1.price > 200 and T2.price > 200
 and C1 = C2

Figure 11: Dynamic view with relation variable.

r(I1)	a0	a1	a2
	v1	u1	w1
	v1	u1	w1
	v2	u2	w1

r(I2)	a0	a1	a2
	v1	u1	w1
	v2	u2	w1
	v2	u2	w1

r'(I)	a2	v1	v2
	w1	u1	u2
	w1	u1	u2

Figure 12: Two instance of r map to the same instance of the view r' .

```
create view r'(a2, ..., a_n, A_0) as
  select T.a2, ..., T.a_n, T.a_1
  from r T, T.a_0 A_0
```

The query defining the view is not an information capacity preserving mapping. To see this, consider the two instances of r (where $n = 2$) depicted in Figure 12. The two instances $I1$ and $I2$ of r map to the same instance I of r' . Hence, any query on r that would return different results for the instances $I1$ and $I2$ does not have an equivalent query on the view r' . This is not to say that r' cannot be used to answer some queries on r .

Example 4.2 Consider Figure 13 containing the definition for the view $db2::nyse$ and a Query $Q2$ on the Schema $db0$ of Figure 10. Suppose we want to use the View $nyse$ to answer $Q2$. $Q2'$ is a possible rewriting of $Q2$ using the view. On the Database $I1$ of Figure 14, $Q2$ and $Q2'$ do not re-

```
create view db2::nyse(date, C) as
  select D, P
  from Db0::stock T, T.exch E,
      T.company C,
      T.date D, T.price P
  where E = 'nyse'
```

Q2: select C1, D1, P1
 from db0::stock T1, T1.date D1,
 T1.company C1, T1.price P1, T1.exch E1
 db0::coType T2, T2.co C2, T2.type Y1
 where E1 = 'nyse' and C1 = C2 and Y1 = 'hitech'

Q2': select C1, D1, P1
 from db1::nyse T1, T1.date D1, db1::nyse->C1
 T1.date C1, T1.C1 P1
 db0::coType T2, T2.co C2, T2.type Y1
 where C1 = C2 and Y1 = 'hitech'

Figure 13: Dynamic view with an attribute variable.

I1

nyse	hp	1/1	100
nyse	hp	1/1	100
nyse	ge	1/1	200

I2

nyse	hp	1/1	100
nyse	ge	1/1	200
nyse	ge	1/1	200

J1

	hp	ge	
	1/1	100	200
	1/1	100	200

Figure 14: Two different instances of $db0$ map to the same instance of the view.

turn the same answer and these queries are therefore not equivalent. Specifically, assuming both ge and hp are hitech stocks, Query $Q2$ issued on the Database $I1$ of Figure 14 will return $I1$ with the exchange attribute projected out. Query $Q2'$ on the same database will return four tuples, $I1$ plus a second copy of the ge tuple. Intuitively, the view loses information about multiplicities. To understand if other rewritings are possible using the view, consider the two databases $I1$ and $I2$ in Figure 14. $Q2$ returns different results in $I1$ and $I2$. The view represents both of these databases with the database $J1$, losing information about the number of copies of a tuple present in the original database.

5 Query Equivalence

To determine the equivalence of queries, we will use an extension of the standard proof technique of establishing containment mappings from V to Q . In [35], the mappings are expressed from columns of V to columns of Q . This is pos-


```

v2 create view s1::stock (co, date, price) as
    select R, D, P
    from s2->R, R T, T.date D, T.price P

v3 create view s1::stock (co, date, price) as
    select A, D, P
    from s3::stock->A, S3::stock T, T.date D, T.A P
    where A <> 'date'

```

Figure 15: Example dynamic views.

sible since in SQL, the columns (domain variables) contain all data that will appear in the query result. We extend this mapping to all variables in a dynamic view. In the following, Q is an SQL query on the schema I .

Let $TV(Q)$ denote the set of tuple variables in Q . For each $T_i \in TV(Q)$, $Table(T_i)$ is a relation in I . $Tables(Q) = \{Table(T_i) | T_i \in TV(Q)\}$ is a multi-set of tables used in Q .

Let $DV(Q)$ denote the set of domain variables in Q . For each $D_i \in DV(Q)$, D_i is declared to range over some attribute domain in the set $\{T_k.A_j | T_k \in TV(Q) \text{ and } A_j \text{ an attribute of } Table(T_k)\}$.

To make our notation simpler, we will assume that all SQL and dynamic queries explicitly declare all tuple and domain variables. That is, relation names are not used as shorthands for tuple variables and relation names (or tuple variables) prefixed with an attribute names are not used as shorthands for domain variables. We give two example dynamic views, that follow these conventions in Figure 15. These views are equivalent to the views of Figure 2.

The variables of Q are then $Var(Q) = DV(Q) \cup TV(Q)$.

Let $Sel(Q) \subseteq Var(Q)$ be the set of variables appearing in the select clause of Q . The predicates used in the where clause are denoted by $Conds(Q)$.

For a view V with a dynamic schema, the schema components include data that must be mapped in considering variable mappings. Let $Db(V)$ be the database specified in the view definition and $Rel(V)$ be the name of the view table. In a dynamic schema, $Db(V)$ and $Rel(V)$ may be variables or constants. $Att(V)$ is the set of names of attributes in the view table. Each $A \in Att(V)$ may be a variable or constant. For each $A \in Att(V)$, $Dom(A)$ denotes the variable from the select clause of the view that provides domain values for A . The variables in $Db(V) \cup Rel(V) \cup Att(V)$ are referred to as *view variables*. The output variables of a view, $Out(V)$, are the view variables and $Sel(V)$.

Definition 5.1 (Variable mapping) A variable mapping from a query $Q1$ to a query $Q2$ is a mapping ϕ from $Var(Q1)$ to $Var(Q2)$ such that if $R(A_1, \dots, A_n) \in Tables(Q1)$ with tuple variable $T1$, there exists a table $R(B_1, \dots, B_n) \in Tables(Q2)$ with tuple variable $T2$ and $B_i = \phi(A_i)$, $1 \leq i \leq n$, $T2 = \phi(T1)$.

The mapping ϕ is 1-1 if every variable of $Q1$ maps to a unique variable of $Q2$. To simplify the presentation, we assume the integration does not contain nul values. However, this restriction is not required [29].

5.1 Select-Project-Join Queries

We first consider queries involving only select, project and join operations (select, from and where clauses without aggregate functions in SQL), or SPJ queries. The queries may have built-in predicates ($\leq, >$) used in the where clause of the query. In considering whether a view V can be used by Q , one must ensure the following conditions [35].

- V does not project out any columns needed in Q
- V does not discard any tuples needed by Q

5.1.1 Set Semantics

We first state the conditions for an SPJ view to be set usable in answering an SPJ query.

Theorem 5.1 [25] *Let Q be an SPJ SQL query and let V be an SPJ SQL view. Then V is set usable in Q if:*

1. *There exist a variable mapping ϕ from V to Q .*
2. *For all $A \in Sel(Q)$ such that $A \in \phi(Var(V))$, either $\phi^{-1}(A) \in Sel(V)$ or there exist a $B \in Sel(V)$ such that $Conds(Q)$ implies $A = \phi(B)$.*
3. *There exist a boolean combination of built-in predicates, $Conds'$ such that*
 - (a) $Conds(Q) \equiv \phi(Conds(V)) \wedge Conds'$
 - (b) $Conds'$ uses only the variables in $\phi(Sel(V)) \cup (Var(Q) - \phi(Var(V)))$.

If V is a dynamic view, then schema components in the view may contain data used for the query. Hence, data returned by Q may originate either from data returned by V (and contained in the attributes of $Sel(V)$) or from schema components in V (and contained in the schema variables of V). For dynamic views, the following conditions must be ensured.

- V does not discard any databases, relations, or attributes needed by Q .
- V does not lose any association between values needed in Q .

Theorem 5.2 *Let Q be an SQL SPJ query and let V be a dynamic SPJ view. Then V is set usable in Q if:*

1. *There exist a variable mapping ϕ from V to Q .*
2. *For all $A \in Sel(Q)$ such that $A \in \phi(Var(V))$, either $\phi^{-1}(A) \in Out(V)$ or there exist a $B \in Out(V)$ such that $Conds(Q)$ implies $A = \phi(B)$.*
3. *There exist a boolean combination of built-in predicates, $Conds'$ such that*
 - (a) $Conds(Q) \equiv \phi(Conds(V)) \wedge Conds'$
 - (b) $Conds'$ uses only the variables in $\phi(Out(V)) \cup (Var(Q) - \phi(Var(V)))$.

Example 5.1 *In Example 4.2, we can use the following mapping ϕ to show equivalence. $\phi(T) = T1$, $\phi(E) = E1$, $\phi(D) = D1$, $\phi(C) = C1$, $\phi(P) = P1$. $Conds' = (C1 = C2 \wedge Y1 = 'hitech')$.*

5.1.2 Multi-Set Semantics

Under set semantics, the mapping may be many to one. In such a mapping, all associations between relevant tuples are preserved. However, multiplicities of tuples are not necessarily preserved. This observation motivates the following result from [35].

Theorem 5.3 [35] *Let Q be an SPJ query and let V be an SPJ view. Then V is multi-set usable in Q if the conditions of Theorem 5.1 hold and ϕ is one-to-one.*

However, the same result does not carry over as directly to dynamic views. As we saw in Example 4.2, the use of attribute variables in a dynamic view can cause multiplicity information to be incorrect. Even if a query uses only attributes that are not dynamic, or relation and database names, the information needed to correctly answer a query may be lost in the view.

Theorem 5.4 *Let Q be an SPJ query and let V be a dynamic SPJ view. Then V is multi-set usable in Q if the conditions of Theorem 5.2 hold, V does not contain any attribute variables and ϕ is one-to-one.*

5.1.3 Query Translation

The query translation algorithm replaces all tables covered by the view with the view schema, mapping variables in the view schema to the appropriate variables used in the query. If the view is dynamic, some of the variables in the rewritten query may be schema variables. The algorithm must be careful to properly declare these variables according to SchemaSQL syntax.

Algorithm 5.1 *Translation of SQL Query Q , to Query Q' using V .*

1. Replace all tables covered by the view with the view schema in the **from** clause.
 - (a) Remove $\phi(\text{Tables}(V))$.
 - (b) If $\text{Db}(V)$ is a variable, then add the declaration $\rightarrow \phi(\text{Db}(V))$.
 - (c) If $\text{Rel}(V)$ is a variable, then add $\phi(\text{Db}(V)) \rightarrow \phi(\text{Rel}(V))$.
 - (d) Add $\phi(\text{Rel}(V))$ T where T is a new tuple variable not used in Q .
 - (e) For each attribute $A \in \text{Att}(V)$, if A is a variable, then add $\phi(\text{Db}(V)) :: \phi(\text{Rel}(V)) \rightarrow \phi(A)$ and $T.\phi(A) \phi(\text{Dom}(A))$.
2. Replace each variable $A \in \text{Sel}(Q)$ by $\phi(B)$ where $B \in \text{Out}(V)$ and $\text{Conds}(Q)$ imply that $A = \phi(B)$.
3. Replace $\text{Conds}(Q)$ in Q by Conds' where $\phi(\text{Conds}(V)) \wedge \text{Conds}' \equiv \text{Conds}(Q)$.
4. For each $A \in \text{Att}(V)$ where $\phi(\text{dom}(A))$ is used in the select or where clause of Q , add $\phi(\text{dom}(A)) \neq \emptyset$ to the where clause of Q' .

5.2 Aggregate Queries and Aggregate Views

We now consider the use of dynamic aggregate views to answer aggregate SQL queries. For economy of presentation, we do not present the full details of the mappings and query translation [29]. Instead, we present a few examples highlighting the major issues involved in using dynamic views with aggregation to answer queries (which may also include aggregates).

We have shown that the restructuring of data in relation and database names in a dynamic view does not lose associations between tuples or multiplicities of tuples. Dynamic views with relation and database variables can therefore be used in much the same way as static views with minor extensions to the query translation algorithm. Dynamic views involving attribute variables (dynamic attribute views) proved to be more problematic. While retaining relevant associations between values, multiplicities of values may be lost. This fact limits the use of these views in answering multi-set queries. Theorem 5.4 appears to be quite a weak result since it does not permit the use of dynamic views with attribute variables in answering queries where the number of values appearing in the result must be preserved. However, dynamic views with attribute variables can be used to answer some aggregate queries.

First, a dynamic attribute view without aggregation can be used to answer aggregate queries that do not require multiplicity information.

Example 5.2 *Consider the following aggregate query on the data of Example 4.2. The proposed rewriting Q' is multi-set equivalent to Q .*

Q select D, max(P) from db0::stock T, T.date D, T.price P, T.exch E where E = 'nyse' group by D having min(P) > 100	Q' select D, max(P) from db1::nyse T, T.date D, db1::nyse \rightarrow A, T.A P group by D having min(P) > 100
---	---

This result follows from the set semantics of aggregates. Our second example shows that dynamic attribute views, where the dynamic attribute is defined using aggregation, can be used to answer aggregate queries.

```

create view db4::E(date, C)
select D, avg(P)
from db0::stock T,
T.exch E, T.company C
where D > 1980
group by E, D, C

```

Example 5.3 *Query Q below can be rewritten to the equivalent query Q' that uses the following aggregate query.*

Q select E, C, avg(P) from db0::stock T, T.exch E, T.company C, T.price P, T.date D where D > 1990 group by E, C	Q' select E, A, avg(P) from db4 \rightarrow E, db4::E \rightarrow A, E T, T.date D, T.A P where D > 1990 group by E, A
--	---

6 Integration with a Query Optimizer

The usability criteria and query translation algorithms of the previous section permit the selection of views that can correctly be used to answer a query. However, they do not address the issue of optimizing queries over a set of views. For SPJ queries and views, this issue has been addressed [8, 37] by extending the common dynamic programming style optimizer [34] to consider plans using views. Two primary extensions are necessary. First, in addition to access methods to base relation, the optimizer must consider the use of views to build a query plan. These views may in turn describe index structures. Second, it must be possible to quickly determine what portion of a query a view answers and whether a plan built from views and other access methods is a partial or complete answer to the query.

A conventional optimizer begins by finding execution plans for single relations, then iteratively finds execution plans for successively larger portions of a query. In the presence of materialized views or indices described by views, the initial set of access plans is extended to include these views. Chaudhuri et al [8] show how for SPJ views, a simple data structure can be used to record the portion of the query answered by the view. This is possible because an SPJ view will replace (or answer) a set of tables and predicates in the query and possibly add a new set of predicates (*Conds* from the translation algorithm). Using only these sets (tables and predicates answered by the view and new predicates added as a result of the view), the optimizer can determine whether a plan using a set of views is partial or complete. For partial plans, the set of tables and predicates that remain to be addressed can be computed.

We have shown that for dynamic SPJ views, the portion of a query answered by a view can also be modeled in the same way. That is, the query translation process involves determining a set of tables and predicates from the query that can be replaced by the view. A query optimizer can therefore treat dynamic views as primitive access plans regardless of whether the view is implemented by an external data source or by an internal index. The higher order properties of the view must be analyzed to determine if the view is usable but additional analysis of this information is not required by the optimizer. In particular, only the index or external source needs to be able to execute the, possibly higher order, plan.

Note that this form of integration with a query optimizer permits correct use of dynamic views while requiring minimal extensions to the optimizer.

7 Conclusions

The existence of schematic heterogeneity in legacy systems is well document in the research literature. Many of the more than thirty representations for a single data fact, enumerated by Kent result from some type of schematic heterogeneity [19]. Despite its prevalence, and despite the plethora of work on enumerating and categorizing types of schematic heterogeneity, no systematic study of how this schematically heterogeneous structures can be used and queried in practice has been undertaken. We have provided a first step in such a study. Specifically, we have analyzed the properties of restructuring transformations required to resolve schematic discrepancies. Using this analysis we have showed how higher order views can be used in answering queries on schematically heterogeneous structures. We have showed that our solution is powerful enough to meet the needs of

numerous applications drawn from the realms of data warehousing, decision support, database publishing and physical data independence. The solutions allow access methods for semi-structured and unstructured data to be incorporated into the framework of structured query evaluation and optimization.

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